

# Crystallization of Poly(butylene terephthalate) from the Glass

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**ABSTRACT:** Crystallization from the glass of poly(butylene terephthalate) (PBT) has been investigated by small-angle X-ray scattering and differential scanning calorimetry. When PBT crystallizes from the glassy state, the nodule crystalline structures in nanometer scale forms and the micrometer order objects, i.e., spherulites, are not observed. The nodule size grows and saturates at a given annealing temperature and increases with increasing annealing temperature. Two temperatures are obtained by the linear extrapolation of the temperature dependence of the reciprocal nodule size to naught. The equilibrium melting temperatures by the Gibbs–Thomson plot, i.e., the melting temperature versus reciprocal nodule size, are also the same temperatures. The lower extrapolated temperature corresponds to the equilibrium melting temperature of the  $\alpha$ -form of PBT. The higher extrapolated temperature is discussed on the basis of the Strobl crystallization model and can be regarded as the equilibrium mesophase–crystal transition temperature.

## 1. Introduction

Poly(butylene terephthalate) (PBT) has two triclinic crystalline forms, the  $\alpha$ -form and the  $\beta$ -form.<sup>1–7</sup> The  $\alpha$ -form crystalline structure is mainly obtained when PBT is crystallized from the molten state or the glassy state. The  $\beta$ -form structure forms when the  $\alpha$ -form crystalline structure is held under strain, and transforms reversibly to  $\alpha$ -form on removal of the strain. The  $c$ -axis (fiber axis) length of the  $\alpha$ -crystalline unit cell, ca. 11.6 Å, is shorter than that of  $\beta$ -form, ca. 13.0 Å, because the conformations of four methyl groups in  $\alpha$ - and  $\beta$ -forms are gauche–trans–gauche and all-trans conformations, respectively.

PBT forms a mesomorphic phase, which has an intermediate structure between crystal and amorphous, in addition to the crystalline forms when an amorphous PBT is stretched at room temperature.<sup>8</sup> The mesomorphic phase has been regarded as a smectic structure by the discoverer. The smectic structure transforms into  $\alpha$ -form by heating. The length of the smectic periodicity is 11.69 Å, which corresponds to the  $c$ -axis length of  $\alpha$ -crystalline unit.<sup>8</sup> A similar mesomorphic phase has been found in other polyesters,<sup>9–15</sup> isotactic polypropylene (iPP),<sup>16–19</sup> and syndiotactic polypropylene (sPP).<sup>20,21</sup> For poly(ethylene terephthalate) (PET)<sup>9–13</sup> and poly(ethylene naphthalate) (PEN),<sup>14</sup> the mesomorphic phases are formed only by stretching the glass. For poly(butylene naphthalate) (PBN),<sup>15</sup> iPP<sup>16–19</sup> and sPP<sup>20,21</sup> the mesomorphic phases are formed by rapid quenching from the molten state as well as by stretching in the glassy state. Such a mesomorphic phase has been also defined as conformationally disordered (condis) crystal or solid mesophase.<sup>22</sup> In this report, a mesomorphic phase is called a smectic structure.

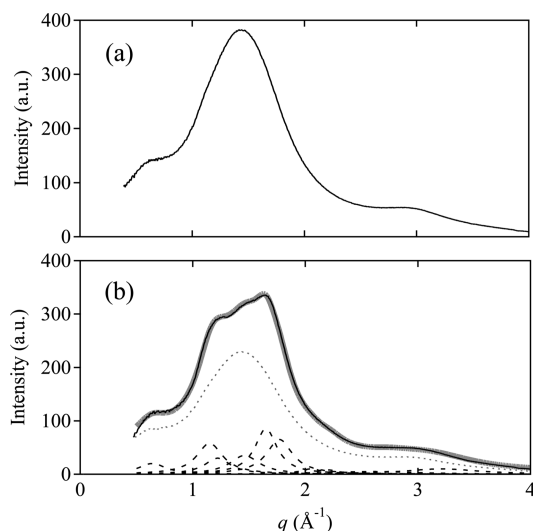
For PBT two glass transition temperatures,  $T_g$ , have been reported as 41 and 102 °C by temperature-modulated differential scanning calorimetry (TMDSC).<sup>23</sup> The lower and the higher  $T_g$ 's are defined as those of a mobile-amorphous, i.e., a normal liquid,  $T_g^{\text{mobile}}$ , and a rigid-amorphous fraction,  $T_g^{\text{RAF}}$ , respectively. A rigid-amorphous fraction exists around the crystallites below  $T_g^{\text{RAF}}$  and is related to the stress transmitted across the crystal

to amorphous interface.<sup>23</sup> A rigid-amorphous fraction disappears above  $T_g^{\text{RAF}}$ .

The crystallization mechanism of PBT has been studied by many methods.<sup>23–33</sup> For example, Hsiao reported the isothermal crystallization in PBT from the melt by the time-resolved simultaneous small-angle X-ray scattering (SAXS) and wide-angle X-ray diffraction (WAXD) methods.<sup>31</sup> Because the crystallization rate of PBT is faster than that of PET,<sup>23,32</sup> however, the behavior of the crystallization mechanism at a large quenching depth and the crystallization mechanism from the glass has not been clarified. In the case of iPP, the spherulites appear on crystallization from the molten state. The molten iPP transforms into the smectic structure by quenching to 0 °C, and the morphology of the smectic structure is a so-called “nodule” structure whose diameter is ca. 100 Å at room temperature.<sup>33–35</sup> The obtained film of the smectic iPP is transparent. The smectic structure transforms into  $\alpha$ -crystalline form of the nodular morphology by heating.<sup>33–36</sup> The nodule size grows and saturates at a given crystallization temperature,  $T_c$ , and increases with increasing annealing temperature.<sup>36</sup> Thus, the formation of spherulites is inhibited in the crystallization process of iPP from the smectic structure.

Recently Strobl has proposed an improved crystallization model through a transient mesomorphic phase.<sup>37,38</sup> According to the model, when a polymer material crystallizes from the molten state, first granular domains of mesomorphic phase form, then transform into the crystalline domains and finally form the lamellar structure. The model also predicts that the extrapolation of temperature dependence of the size of crystal gives a virtual transition between the mesomorphic phase and the crystal, and that the equilibrium mesomorphic–crystal transition temperature,  $T_{MC}^\infty$ , is located above the equilibrium melting temperature of crystal,  $T_m^\infty$ .<sup>38</sup> In order to clarify the crystallization mechanism of PBT which forms the smectic structure by stretching at a large quenching depth, we have investigated the crystallization from the glass of PBT by SAXS and differential scanning calorimetry (DSC). In this report, we obtain  $T_m^\infty$  from the relation between  $T_m$  and the size of crystallite by SAXS and DSC and discuss whether Strobl's model is applicable to the crystallization mechanism of PBT from the glass in the present experimental results.

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**Figure 1.** WAXD of (a) the quenched PBT and (b) the PBT annealed at 30 °C for 30 min from the quenched state. The solid line in (b) shows the observed intensity and the thick gray line, the fitting curve. The latter is reproduced by summing up the components of the  $\alpha$ -form (broken line) and amorphous phase (dotted line).

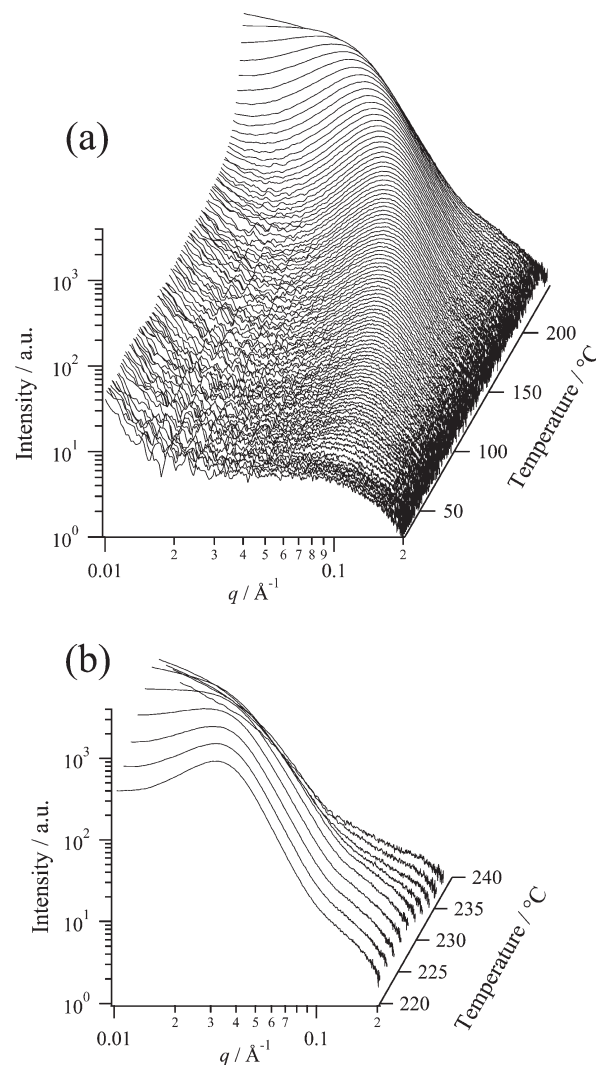
## 2. Experimental Section

The polymer used in this study was PBT with  $M_v = 38\,000$  purchased from Sigma-Aldrich Co. Ltd. PBT was melted at ca. 280 °C for 2 min on a hot-plate, and then rapidly quenched in ice–water. The thickness of the quenched PBT film is ca. 150  $\mu\text{m}$ . The quenched PBT film was measured by wide-angle X-ray diffraction (WAXD) immediately after quenching. The PBT film annealed at 30 °C for 30 min heated from 0 °C was also measured by WAXD. The time-resolved SAXS measurements were carried out in the heating process and the isothermal crystallization process for the quenched PBT. In the heating process the PBT sample was heated from 30 to 260 °C at a rate of 10 °C/min after annealing at 30 °C for 5 min. In the isothermal crystallization the PBT samples were heated from room temperature at the rate of 100 °C/min, and then were isothermally crystallized at  $T_c = 40, 60, 80, 100, 120, 140, 160, 180,$  and 200 °C. In order to ensure the scattering intensity the sample films were plied 2-fold. The heating process of PBT sample after annealing at  $T_c$  (30–225 °C) for  $t_c$  (5–120 min) was analyzed by DSC for comparison with the SAXS measurements.

WAXD measurements were performed using the Rigaku Rint 2500 system. The WAXD patterns were recorded using an imaging plate which covers the  $q$ -range from 0.4 to 4  $\text{\AA}^{-1}$  ( $q = 4\pi(\sin \theta)/\lambda$ ;  $\lambda$  and  $2\theta$  being X-ray wavelength and scattering angle, respectively). The value of  $\lambda$  in WAXD was 1.54  $\text{\AA}$ . SAXS measurements were performed using the beamline BL-45XU at SPring-8, Nishiharima, Japan. The SAXS covers the range of scattering vector  $q$  from 0.08 to 0.2  $\text{\AA}^{-1}$ . The value of  $\lambda$  in SAXS was 0.9  $\text{\AA}$ . The temperature of the samples for the SAXS measurements was controlled using a Linkam LK-600PH. The DSC measurement was carried out in the heating process of the PBT samples with Shimadzu DSC60 at a rate of 10 °C/min in the range from –10 to +280 °C.

## 3. Results and Discussion

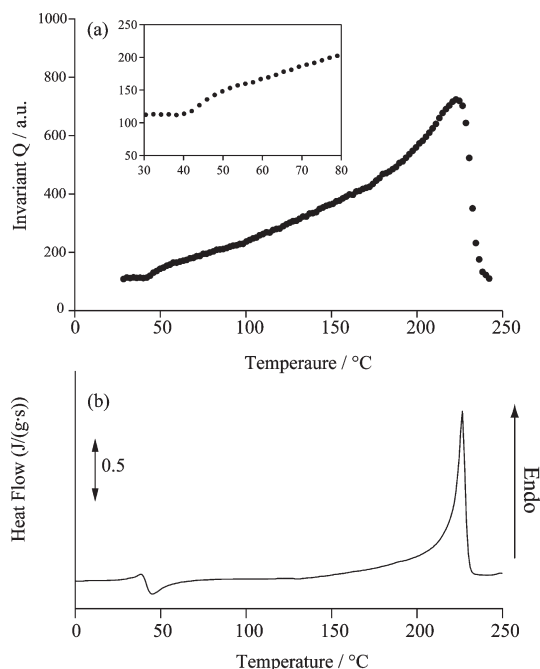
**3.1. Structures of PBT Crystallized from the Glass.** Figure 1 shows the WAXD diagrams of the PBT quenched from the molten state to 0 °C and the PBT's annealed at 30 °C for 30 min from the quenched state. The structure of the PBT as quenched is identified as the amorphous phase because of the existence of an amorphous halo only. The PBT annealed at 30 °C has a fraction of  $\alpha$ -form because the broad Bragg peaks of  $\alpha$ -form at  $q = 0.64, 1.15, 1.22, 1.46, 1.65, 1.77, 2.05, 2.20,$  and 3.22  $\text{\AA}^{-1}$  are



**Figure 2.** SAXS profiles of a heating process for the PBT annealed at 30 °C for 30 min from the quenched state at a rate of 10 °C/min: (a) from 30 to 220 °C; (b) from 220 to 240 °C.

observed in Figure 1b. The peaks were fitted to the Lorentzian functions. The crystallinity of the annealed PBT in Figure 1b was calculated using an area ratio of the sum of the fitting peaks to the observed diagram and was obtained as 35%. The annealed PBT film is transparent despite crystallization. Micrometer order objects, i.e., spherulites, are not observed during the heating process from the glass to the melt by an optical microscope. Thus, the crystallization from the glass of PBT forms the nanometer order objects, i.e., the nodular structure, rather than spherulites composed of lamellar crystals.

Figure 2 shows the SAXS intensities  $I(q)$  of the quenched PBT during the heating process from 30 to 260 °C. The SAXS curve at 30 °C has a weak peak at  $q_{\text{max}} \approx 0.09 \text{ \AA}^{-1}$ , corresponding to ca. 70  $\text{\AA}$ . According to the WAXD results, already the PBT annealed 30 °C is semicrystalline. Therefore, the observed SAXS peak is related to a nanoscale correlation among the corresponding entities and the entities are crystalline. The ensemble of nanoscale entities is regarded as a nodule structure similar to the one which is observed in iPP quenched from the melt to 0 °C.<sup>33–35</sup> Manabe and co-workers have studied the morphology of PBT isothermally crystallized at 40 °C from melt by transmission electron microscopy.<sup>39</sup> They have observed granule-like crystalline domains with indistinct boundary in the PBT sample.



**Figure 3.** (a) Temperature dependence of invariant  $Q$  calculated from the results of the SAXS profiles in Figure 2. (b) DSC curve of a heating process at a rate of 10 °C/min for the PBT annealed at 30 °C for 30 min from the quenched state.

The peak shifts to the lower  $q$  side and the intensity  $I_{\max}$  at  $q_{\max}$  increases with increasing annealing temperature.

In order to clarify the structural change during the heating process, we calculate the invariant  $Q$  defined by<sup>40</sup>

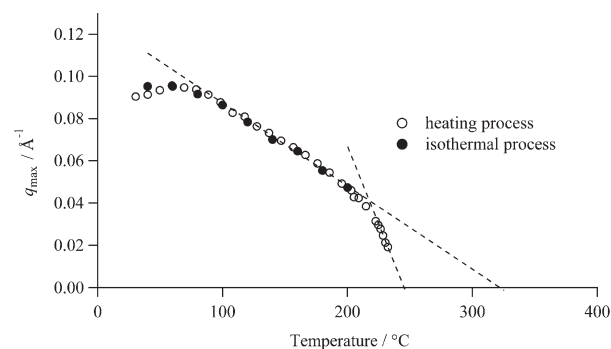
$$Q = \int_0^\infty 4\pi q^2 I(q) dq = (\rho_c - \rho_a)^2 \phi_c (1 - \phi_c) \quad (1)$$

where  $\phi_c$  is crystallinity, and  $\rho_c$  and  $\rho_a$  are the densities of crystal and amorphous, respectively. Figure 3a shows the invariant  $Q$  calculated from the SAXS results in Figure 2. The  $Q$  value remains nearly constant below 40 °C, increases from 40 to 224 °C, and then decreases. The behavior of the  $Q$  shows that the PBT further crystallizes from 40 °C and the crystalline structure melts at 224 °C during the heating process of the PBT annealed at 30 °C from the glassy state. Figure 3b shows the DSC curve of the heating process of the quenched PBT annealed at 30 °C for 30 min in order to compare to the behavior of the  $Q$  value. The curve shows endothermic peaks at 38 and 226 °C and an exothermic peak at 45 °C. The peak at 226 °C is obviously identified as the melting peak and corresponds to the value of  $T_m$  from the behavior of the  $Q$  value. The endothermic and exothermic peaks at 38 and 45 °C have been identified as the melting peak and the crystallization peak to  $\alpha$ -form, respectively.<sup>32</sup> These peaks shift to higher temperature positions with increasing annealing temperature.<sup>32</sup>

**3.2. Change in Nodule Structure Size and the Equilibrium Melting Temperature.** The morphology of crystalline part in a semicrystalline polymer material is usually observed as a lamellar structure. The melting temperature  $T_m$  of the crystal depends on the lamellar thickness  $l$  and the relationship between  $T_m$  and  $l$  is given by<sup>40</sup>

$$l^{-1} = \Delta H(T_m^\infty - T_m) / 2\delta_e T_m^\infty \quad (2)$$

where  $\Delta H$ ,  $T_m^\infty$ , and  $\delta_e$  are the heat of fusion, the equilibrium



**Figure 4.** Temperature dependence of  $q_{\max}$  obtained from the SAXS results in the heating process (open circles) and the isothermal process (closed circles).

melting temperature and the specific energy of chain-folded surface, respectively. Furthermore, it is well-known that the lamellar thickness  $l$  also depends on a crystallization temperature  $T_c$ , and from theoretical,<sup>41</sup> experimental,<sup>42–45</sup> and simulation<sup>46,47</sup> evidence the relationship between  $T_c$  and  $l$  is given by

$$l^{-1} \sim (T_c^\infty - T_c) \quad (3)$$

where  $T_c^\infty$  denotes a temperature at which an infinite lamellar thickness forms.

Figure 4 shows the temperature dependence of the  $q_{\max}$  of SAXS curves in Figure 2. During the heating process of the quenched PBT,  $q_{\max}$  slightly increases until 70 °C, decreases above 70 °C, and then decreases more drastically above 210 °C. The values of  $q_{\max}$  in the high temperature region from 210 to 230 °C are extrapolated to 245 °C, which well corresponds to the  $T_m^\infty$  reported by Chen and co-workers.<sup>32</sup>

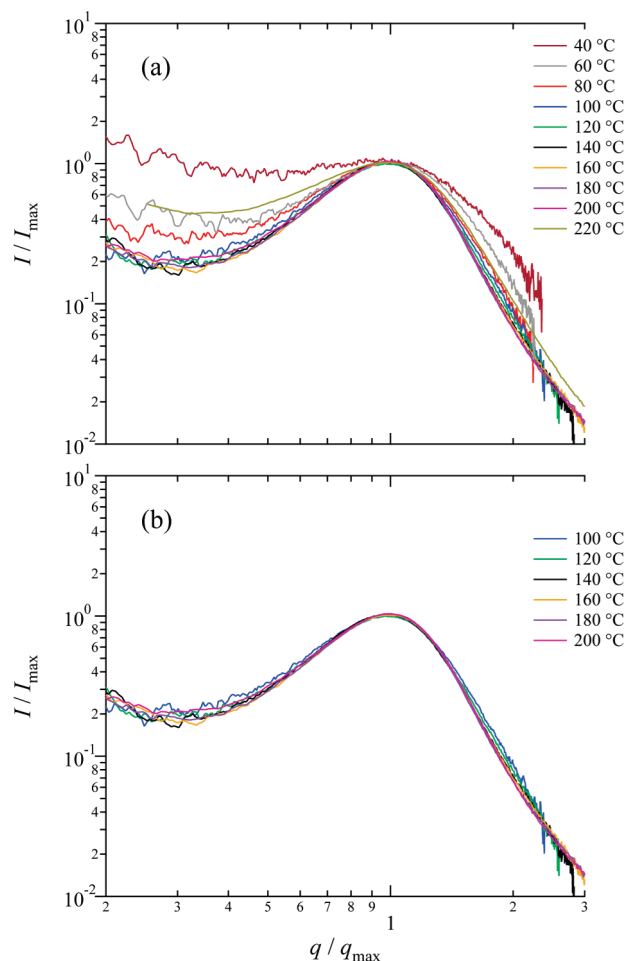
A scattering function for a system of dispersed particles is described by the product of structure factor and form factor. The value of  $q_{\max}$  is generally given by the combination of the internodule distance  $\Lambda$  and the nodule size  $d$ . When the scatterers are densely packed in space as suggested by the crystallinity of 35% in the present case, however,  $q_{\max}$  is approximately given by

$$q_{\max} \approx 2\pi/\Lambda \quad (4)$$

Parts a and b of Figure 5 show the SAXS profiles during the heating process normalized by  $q_{\max}$  and  $I_{\max}$ . The normalized SAXS profiles at all temperatures in Figure 5a do not give a master curve, but those between 100 and 200 °C in Figure 5b give a master curve. When the scattering functions normalized by  $q_{\max}$  and  $I_{\max}$  give a master curve, the structures are similar. Therefore, the nodule structures between 100 and 200 °C can be scaled by  $\Lambda$ , which indicates that the ratio of  $d$  to  $\Lambda$  and hence  $\phi_c$  is constant in this temperature range. The increase in  $Q$  between 100 and 200 °C can be interpreted in terms of the difference in the thermal expansion coefficients between crystal and amorphous phase, i.e., the factor  $(\rho_c - \rho_a)^2$  in eq 1.<sup>4,24,30</sup> Here, we will apply eq 3 to the case of the nodule structure by substituting  $q_{\max}$  for  $l^{-1}$  (see section 3.5):<sup>36</sup>

$$q_{\max} \sim (T_c^\infty - T_c) \quad (5)$$

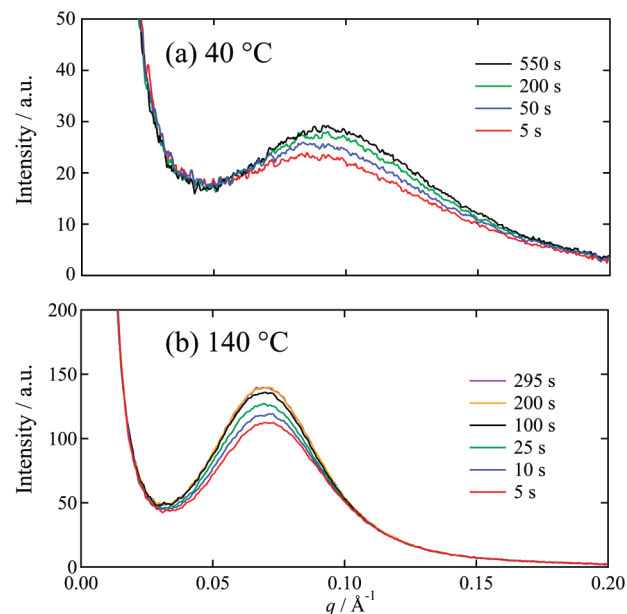
In Figure 4, a straight line can be drawn from the temperature dependence of  $q_{\max}$  between 100 and 200 °C and is extrapolated  $T_c^\infty = 330$  °C, which is 85 °C higher than  $T_m^\infty$ . Here  $T_c^\infty = 330$  °C is obtained from the temperature dependence of  $d$  between 100 and 200 °C and  $T_m^\infty = 245$  °C is obtained from that of  $\Lambda$  above 220 °C. The crossing point of



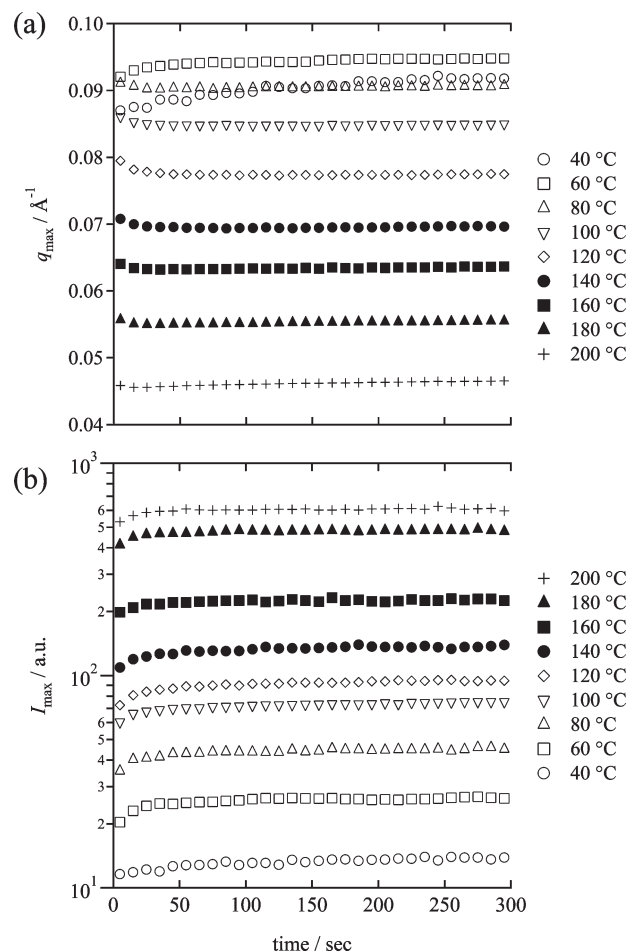
**Figure 5.** SAXS profiles normalized by  $q_{\max}$  and  $I_{\max}$  collected during the heating process of the quenched PBT at a rate of 10 °C/min in the temperature ranges (a) from 40 to 220 °C and (b) from 100 to 200 °C.

two straight lines drawn from the temperature dependence of  $q_{\max}$  below 200 °C and above 220 °C in Figure 4 is 215 °C.

We examined the SAXS behavior in the isothermal process of the quenched PBT in order to compare to the  $q_{\max}$  value of the heating process of the quenched PBT. Parts a and b of Figure 6 show the time evolved SAXS curves during the isothermal process at 40 and 140 °C from the glassy state, respectively. The SAXS curves at annealing temperatures higher than 80 °C show that the  $q_{\max}$  slightly shifts to the lower  $q$ -value region immediately after starting annealing and then remains constant, and the intensity  $I_{\max}$  at  $q_{\max}$  increases with time. Figure 7 shows the annealing time dependence of  $q_{\max}$  and  $I_{\max}$  of SAXS profiles during the isothermal processes at 40, 60, 80, 100, 120, 140, 160, 180, and 200 °C. The  $q_{\max}$  of isothermal process at 40 °C increases gradually with time. The  $q_{\max}$  at 60 °C also increase gradually with time but faster than that at 40 °C. However, the  $q_{\max}$  at each annealing temperature above 60 °C immediately shifts to the value determined by the temperature and remains unchanged within the annealing time in the present measurements. The  $I_{\max}$  of SAXS profile at each annealing temperature also increases up to a value dependent on temperature. This characteristic behavior suggests the existence of a quasi-equilibrium state for the relation between the nodule structure size and annealing temperature. Such a behavior has been observed in the isothermal crystallization process of iPP from room temperature in which iPP has the smectic



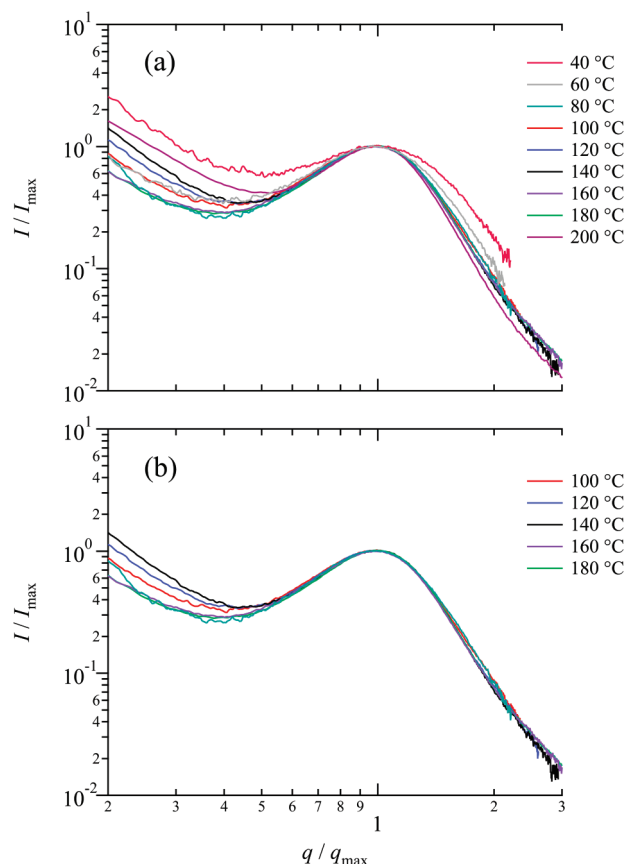
**Figure 6.** Time-resolved SAXS profiles of the PBTs annealed at (a) 40 and (b) 140 °C from the quenched state.



**Figure 7.** Time evolutions of (a)  $q_{\max}$  and (b)  $I_{\max}$  obtained from SAXS profiles of the PBT annealed at several temperatures from the quenched state.

structures.<sup>36</sup> The rate of change in  $I_{\max}$  is slightly slower than that in  $q_{\max}$  for all annealing temperatures. The  $q_{\max}$  of SAXS profiles of the PBTs annealed at 40 and 60 °C for



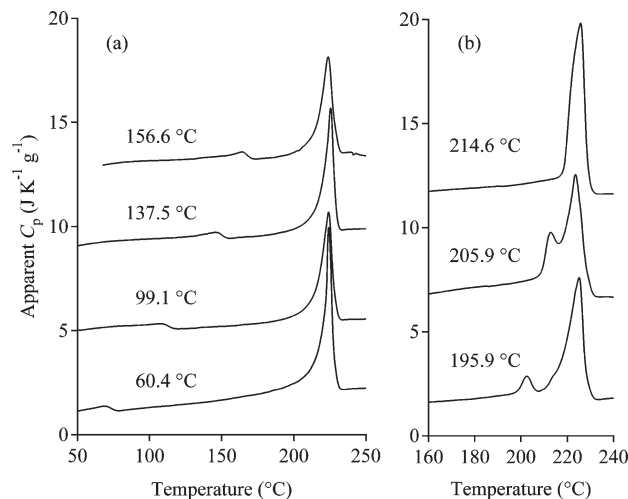


**Figure 8.** SAXS profiles normalized by  $q_{\max}$  and  $I_{\max}$  for the PBT annealed at different temperatures for 200 s from the quenched state. The temperature ranges are (a) 40 to 200 °C and (b) 100 to 180 °C.

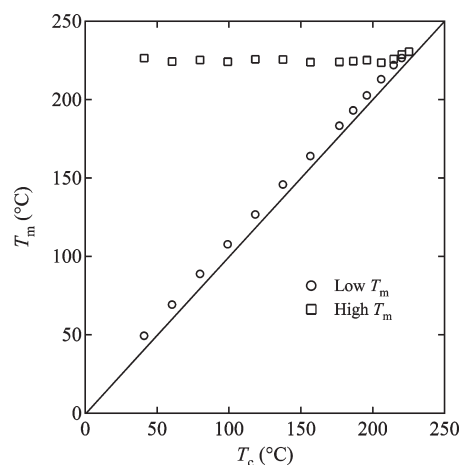
600 s and at 80, 100, 120, 140, 160, 180, and 200 °C for 200 s are plotted in Figure 4. The  $q_{\max}$  in the isothermal processes above 80 °C are the same as those in the heating process.

Parts a and b of Figure 8 show the normalized SAXS profiles during the isothermal process at different temperatures in the range between 40 and 200 °C and between 100 and 180 °C at 200 s normalized by  $q_{\max}$  and  $I_{\max}$ . Although the normalized SAXS profiles in Figure 8a do not give a master curve, the normalized SAXS profiles in Figure 8b superpose except at low  $q$ . The result equally leads that the  $q_{\max}^{-1}$  is proportional to  $d$  between 100 and 180 °C in the isothermal process as in the heating process (Figure 5, parts a and b).  $T_c^\infty = 330$  °C is also obtained from the SAXS results in both the heating process and the isothermal process.

**3.3. The Melting Temperature of the Nodule Structure and the Equilibrium Melting Temperature.** Figure 9 shows the DSC curves of the heating process of the PBT annealed at  $T_c$  for  $t_c = 10$  min from the glass. The DSC curves of the PBT specimen annealed below 215 °C show two endothermic peaks. As mentioned above, the endothermic peaks are identified as the melting peaks. Figure 10 shows the relation between two melting temperatures  $T_m$  and crystallization temperature  $T_c$ . The lower melting temperature exists just above the annealing temperature between 40 and 220 °C. Similar results are reported by Cheng and co-workers.<sup>32</sup> The higher melting temperature might be obtained by the second crystallization during the heating process. Furthermore, from the  $T_m$  values above the 215 °C the  $T_m^\infty$  value is obtained as 245 °C which corresponds to that reported by other research groups.<sup>32</sup>



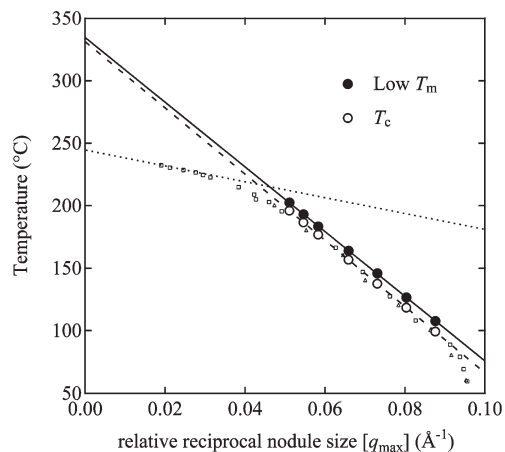
**Figure 9.** DSC curves in the heating process at a rate of 10 °C/min for the PBT annealed at several temperatures for 10 min from the quenched state. The inserted numbers indicate the annealing temperatures,  $T_c$ . The DSC curves are shifted vertically.



**Figure 10.**  $T_c$  dependence of the low and high  $T_m$ 's obtained from the DSC curves in Figure 9 in the heating process for the PBT annealed at  $T_c$  for 10 min from the quenched state.

The SAXS results show that the nodule size is inversely proportional to the  $q_{\max}$  value between 100 and 180 °C (Figures 4 and 8). Thus, the melting temperature,  $T_{m,n}$ , of the nodule structure formed by annealing between 100 and 180 °C can be obtained as lower  $T_m$  in Figure 10, and the equilibrium melting temperature can be estimated by eq 2, i.e., the Gibbs–Thomson plot. Figure 11 shows the relation between the relative reciprocal nodule size defined by  $q_{\max}$  and  $T_m$ . The nodule size on crystallization at  $T_c$  in DSC measurements is estimated from the SAXS result in Figure 4. The extrapolated temperature is  $T_m^\infty = 333$  °C and corresponds to the value of  $T_c^\infty$ , 330 °C, obtained from the SAXS results. However the  $T_m^\infty = \text{ca. } 330$  °C differs substantially from  $T_m^\infty = 245$  °C in Figure 11. The reason for the difference will be discussed subsequently.

**3.4. The Crystalline Morphology below 100 °C and above 200 °C.** From the SAXS results the nodule structure can not be scaled by  $\Lambda$  below 100 °C and above 200 °C. As shown in Figure 10 presenting the relation between  $T_c$ ,  $T_{m,n}$  (lower  $T_m$ ), and  $T_m$  of the crystallite (higher  $T_m$ ), for all  $T_c$  the  $T_{m,n}$  is only slightly above  $T_c$ . This means that even for temperatures below 100 °C the nodule size  $d$  increases with increasing



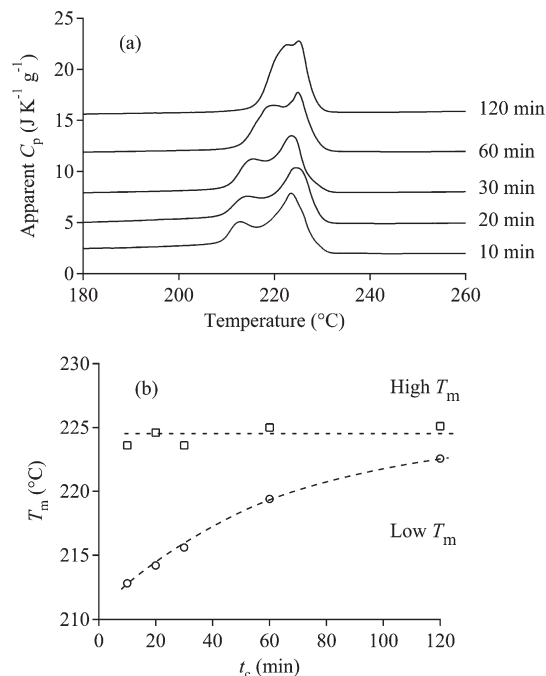
**Figure 11.** Relation between relative reciprocal nodule size and crystallization temperature  $T_c$  (open circles) and low  $T_m$  (filled circles). The relative nodule size obtained by the isothermal process at  $T_c$  is estimated from the SAXS result (Figure 4) and the relative reciprocal nodule size is displayed as  $q_{\max}$  in the figure. Small squares and triangles present the  $q_{\max}$  values in the heating process and the isothermal crystallization process in Figure 4, respectively.

$T_c$ . However Figure 4 shows the  $q_{\max}$  value almost remains unchanged below 100 °C. The results explain that the inter-nodule distance  $\Lambda$  remains in spite of the increase in the nodule size  $d$ . Pyda and co-workers have reported that  $T_g^{\text{RAF}}$  is located at 102 °C.<sup>23</sup> The rigid-amorphous fraction is less mobile layer surrounding the crystal and inhibits a nucleation of a crystal. We consider that  $\Lambda$  is not proportional to  $d$  because the rigid-amorphous fraction that inhibits the nucleation of the nodules exists as the excess space around the nodule structure below  $T_g^{\text{RAF}} = 102$  °C. Above the  $T_g^{\text{RAF}}$ , the rigid-amorphous fraction disappears, the nucleation occurs and the nodule structures can be scaled by SAXS.

Next we discuss the melting behavior above 200 °C. Figure 12a shows the DSC curves of PBT annealed at  $T_c = 205$  °C for several  $t_c$ . The lower  $T_m$  increases with  $t_c$  (Figure 12b). From the DSC result,  $d$  is considered to increase with  $t_c$  in the isothermal process above 200 °C in order to decrease the specific surface of the nodule structures. Thus, we suggest that the reason why the normalized SAXS profiles above 200 °C in Figures 5 and 8 do not give a master curve is the increase in the ratio of  $d$  to  $\Lambda$ .

**3.5. A Crystallization Model through a Metastable State for a Polymer Consisting of a Nodule Structure.** We discuss a crystallization model applicable to the experimental results of PBT having the nodule structure and two extrapolated equilibrium temperatures. Keller and co-workers have presented the orthorhombic crystalline formation of polyethylene (PE) through the hexagonal phase by the thermodynamic treatment.<sup>48,49</sup> At a temperature below the melting temperature of the orthorhombic phase under a pressure below the triple point, the orthorhombic phase is stable and the hexagonal one is metastable. At this temperature and pressure, a crystal first grows in the hexagonal phase, and then the hexagonal phase transforms into the orthorhombic phase when the thickness of the hexagonal phase reaches a thickness thermodynamically stable for the orthorhombic phase. A hypothetical equilibrium transformation temperature  $T_{\text{tr}}$  can be estimated higher than  $T_m^\infty$  of the orthorhombic phase.

Strobl and co-workers<sup>37,38</sup> modified the Keller's treatment and proposed an improved crystallization model through a transient mesomorphic phase based on the experimental evidence<sup>43–45</sup> of syndiotactic polypropylene (sPP),



**Figure 12.** (a) DSC curves of a heating process at a rate of 10 °C/min for the PBT annealed at 205 °C for  $t_c = 10, 20, 30, 60$ , and 120 min from the quenched state. The DSC curves are shifted vertically. (b)  $t_c$ -dependences of peak positions of high and low  $T_m$ 's in part a.

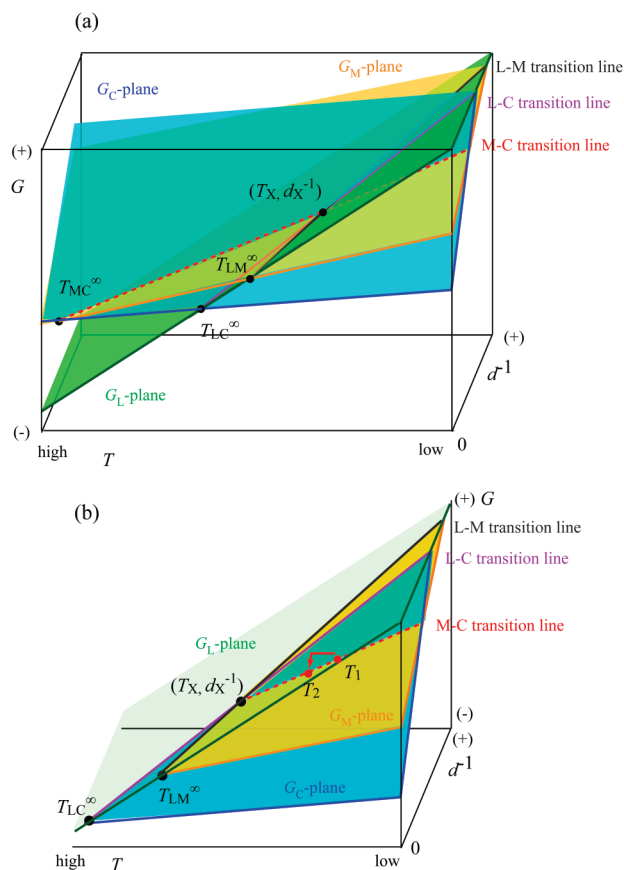
poly( $\epsilon$ -caprolactone), PE and isotactic polypropylene (iPP). The model explains the growth mechanism of crystalline lamellae through the mesomorphic phase:<sup>37,38</sup> (i) The mesomorphic layers form on the growth front of lamellae. (ii) When the mesomorphic layer grows up to a critical size, the mesomorphic layer transforms into the granular crystalline blocks. (iii) The crystalline blocks merge together and finally form the lamellar structure. The model also proposes the existences of the melting temperature of the mesomorphic phase,  $T_{\text{am}}$ , and a virtual transition temperature between the mesomorphic and the crystalline phase,  $T_{\text{mc}}$ .<sup>38</sup>

Here we modify Strobl's model to comply with the nodule structures obtained from the experimental results of PBT. We consider the whole growth mechanism of the nodule structures which exist all over the sample instead of the local growth mechanism on the growth front of lamellar structures. The present crystallization model assumes that the nodule structure grows when the nodule structure is in the mobile mesomorphic phase, and stops growing when the mesomorphic phase transforms into the rather immobile crystalline phase. At a high temperature near  $T_m^\infty$ , however, the crystallization model allows that the crystalline nodule structure further gradually grows in order to decrease the specific surface of the nodule structures.

Figure 13 shows a schematic plot of the free energy,  $G$ , versus temperature,  $T$ , at an ambient pressure for the system having the mesomorphic phase as a metastable state. The subscripts L, M and C denote the liquid, the mesomorphic and the crystalline phase, respectively in the following discussion. The free energies,  $G_M$  and  $G_C$  are dependent on a nodule size,  $d$ . When the nodule structure is infinite  $d = d_\infty$ , the differences between the free energies  $G_L$  and  $G_C$ , between  $G_L$  and  $G_M$  and between  $G_M$  and  $G_C$  at a temperature  $T$  ( $T < T_{\text{MC}}$ ) are given by

$$\begin{aligned} \Delta G_{\text{LC}}(d_\infty) &= G_C(d_\infty) - G_L \\ &= -\Delta H_{\text{LC}}(T_{\text{LC}}^\infty - T)/T_{\text{LC}}^\infty \end{aligned} \quad (6)$$





**Figure 15.** Schematic relationship between free energy  $G$ , temperature  $T$  and inverse characteristic nodule size,  $d^{-1}$ , for the crystalline polymer system having a metastable mesomorphic phase. Key: (a) overall view and (b) enlarged image of  $G_M$  and  $G_C$  below  $G_L$ . The arrow in part b indicates that a nodule grows by heating from  $T_1$  to  $T_2$  in Figures 13 and 14.

dependence of the nodule size below and above the  $T_X$  are M-C and L-C transition lines, respectively. When  $T = T_{LC} = T_{LM} = T_{MC} = T_X$  in eq 12-15,  $d$  becomes  $d_X$  and the relation between  $T_X$  and the other parameters is given by

$$\delta_{MC}/(T_{MC}^\infty - T_X) = \delta_{LC}/(T_{LC}^\infty - T_X) - \delta_{LM}/(T_{LM}^\infty - T_X) \quad (16)$$

Figure 15 shows a schematic 3-dimensional image of  $G$ ,  $T$ , and  $d^{-1}$  for the system having the mesomorphic phase as a metastable state. The lines of intersection of  $G_L$  and  $G_M$  planes,  $G_L$  and  $G_C$  planes and  $G_M$  and  $G_L$  planes are L-C, L-C, and M-C transition lines, respectively. The projections of L-M, L-C and M-C transition lines onto the  $G$ - $T$  plane give Figure 13, and the projections of L-M, L-C, and M-C transition lines onto  $T$ - $d^{-1}$  plane give Figure 14. Figure 15b shows the schematic image of  $G_M$  and  $G_C$  below  $G_L$  and clearly indicates the growth of nodule on heating from  $T_1$  to  $T_2$  in the same way as shown in Figure 13 and 14. Thus, the nodule grows along the M-C transition line by heating up to  $T_X$ , and grows along L-C transition line from  $T_X$  to  $T_{LC}^\infty$ .

We apply the model to the present experimental results of PBT. In PBT, we obtain the extrapolated temperature at 330 or 333 °C, which is ca. 85 °C higher than  $T_{LC}^\infty = 245$  °C, from the crystallization temperature dependences of the nodule size (Figure 4) and of the melting temperature of the nodule (Figure 11) between 100 and 200 °C. Furthermore, the

crossing point of two temperature dependences of the  $q_{\max}$  value in Figure 5 is located at 215 °C. We suggest that  $T_{LC}^\infty$  and  $T_{MC}^\infty$  for PBT are 245 and 333 °C, respectively. Although the accurate value of  $T_X$  is not obtained because the nodule structure can not be scaled above 200 °C from the SAXS results, we also suggest that the temperature  $T_X$  is located at ca. 215 °C. We suggest that the reason for the breakdown of the scaling of the nodule structure above 200 °C (Figures 5 and 8) near  $T_m^\infty$  is that the nodule structure grows gradually from the size given from eq 15 in order to decrease surface energy from the DSC results (Figure 12).

Finally, we consider a possible origin of the transient mesomorphic phase for PBT. Konishi et al. have investigated the structure of the mesomorphic phase of iPP from the viewpoint of the formation mechanism and the crystallization mechanism of iPP from the smectic structure.<sup>19</sup> The structure of the mesomorphic phase has been explained liquid crystal like structure, i.e. a smectic structure by regarding the 3/1 helix as a mesogen.<sup>19</sup> The morphology of the smectic structure is nodular and the smectic structure transforms into  $\alpha$ -crystalline form with the nodular morphology by heating, the size of which increases with increasing annealing temperature. Two kinds of temperature dependence of the nodule size in the crystallization from the smectic structure below and above  $T_c = 125$  °C exist and lead  $T_c^\infty = 270$  and 193 °C, respectively.<sup>36</sup>  $T_c^\infty = 193$  and 270 °C and  $T_c = 125$  °C correspond to  $T_{LC}^\infty$ ,  $T_{MC}^\infty$  and  $T_X$  which are based on the modified Strobl's model, respectively. It has been confirmed that the smectic structure disappears above 125 °C by WAXD.<sup>36</sup> PBT also has the smectic structure by stretching the glass at room temperature. Because the smectic structure also transforms into  $\alpha$ -crystalline form with increasing temperature above  $T_g$ , the smectic structure is a mobile metastable phase. Thus, the smectic structure may play a role of a transient mesomorphic phase in PBT.

#### 4. Conclusion

The crystallization from the glass of PBT has been investigated by SAXS and DSC. The SAXS intensity curve of the PBT shows a long spacing of the nodular crystals of ca. 10 nm. The peak position in the SAXS curves shifts to the lower  $q$ -side with increasing annealing temperature; the nodule size increases with increasing annealing temperature. The relation between the nodule size and annealing temperature leads two extrapolated temperatures  $T_c^\infty$ . Two linear relations between the nodule size and temperature below and above  $T_c = 200$  °C lead  $T_c^\infty = 331$  and 245 °C, respectively. The lower  $T_c^\infty = 245$  °C corresponds to the equilibrium melting temperature  $T_m^\infty$ . The DSC results combined with the SAXS results also show the relation between the nodule size and the melting temperature, and the relation also leads two equilibrium melting temperatures  $T_m^\infty = 334$  °C above 245 °C. The higher  $T_c^\infty = 330$  °C is regarded as the equilibrium mesomorphic-crystalline phase transition temperature on the basis of Strobl's crystallization model.<sup>38</sup> Furthermore, the change of the ratio of the nodule size to the internodule distance below 100 °C and above 200 °C is revealed by considering the normalized SAXS curve and the  $T_m$  behavior of DSC results. Below 100 °C the rigid-amorphous fraction exists around the nodule crystalline structure and inhibits the nucleation of the crystal around the nodule. Above 200 °C near  $T_m^\infty$ , the nodule structure gradually grows in order to decrease the surface energy.

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